

this reason no further discussion is warranted here. The symbol  $\theta_{298}^I$  is used herein to represent the Debye temperature determined from X-ray or neutron diffraction intensity data. The subscript refers to the temperature at which the experimental data were obtained. It should be noted that the experimentally measured  $\theta^{Ie}$  value is not directly comparable with  $\theta^S$ , because these two quantities are defined differently.<sup>96,111</sup> Zener and Bilinsky<sup>111</sup> showed that the ratio of  $\theta^{Ie}/\theta^S$  can be expressed as a function of Poisson's ratio; thus, from the known Poisson's ratio (Table III) of the material whose  $\theta^{Ie}$  has been experimentally determined, one can calculate the  $\theta^I$  value which should be compared with  $\theta^S$ . All of the values given in Tables XVII and XVIII are  $\theta^I$  values; that is, the experimental values  $\theta^{Ie}$  have been converted to  $\theta^I$  by the method of Zener and Bilinsky.

The  $\theta_{298}^I$  values for 17 elements are listed in Table XVII and are compared with  $\theta_{298}^S$  in Table XVIII. It is seen that the  $\theta_{298}^I$  values range from a minimum of 67°K for lead to a maximum of 1730°K for diamond. Examination of the ratio of  $\theta_{298}^I/\theta_{298}^S$  in Table XVIII indicates that only 47% of the  $\theta_{298}^I$  values lie within  $\pm 10\%$  of the corresponding  $\theta_{298}^S$ , and that about 70% lie within  $\pm 25\%$ . Thus the agreement between  $\theta_{298}^I$  and  $\theta_{298}^S$  is poor. Furthermore,  $\theta_{298}^I$  is less than  $\theta_{298}^S$  for about 82% of the elements. Since, as noted earlier,  $\theta_{298}^E \approx \theta_{298}^S$  (i.e., approximately equal numbers of values of  $\theta_{298}^E$  are larger and smaller than  $\theta_{298}^S$ ) and since  $\theta_{298}^I < \theta_{298}^S$ , it is concluded that  $\theta_{298}^I$  is generally less than  $\theta_{298}^E$ . This is in agreement with the observations of Blackman<sup>93</sup> and Herbstein.<sup>96</sup>

#### IX. Some Interrelationships and Derived Properties

#### 22. RATIO OF YOUNG'S MODULUS TO THE SHEAR MODULUS

The ratio of Young's modulus to the shear modulus,  $Y/\mu$ , is essentially a constant for all materials. This is quite easily seen from Eq. (II.1) or (5.1), which show that  $Y/\mu$  is related to Poisson's ratio. Since Poisson's ratio is practically a constant, equal to 0.301 (see Section 5), we find  $Y/\mu = 2.604$  from Eq. (5.1). Furthermore, since Poisson's ratio can only have values between 0 and 0.5, the minimum value for  $Y/\mu$  is 2.0 and the maximum is 3.0. Poisson's ratio is usually measured directly and not calculated from the two moduli; thus the interrelationships, as given by Eq. (II.1) or (5.1), among the three quantities serve as a check on the consistency of the three measured values.

The  $Y/\mu$  ratios, which are listed in Table XIX, were calculated from

<sup>111</sup> C. Zener and S. Bilinsky, *Phys. Rev.* **50**, 101 (1936).

TABLE XIX. RATIO OF YOUNG'S MODULUS TO THE SHEAR MODULUS

Element	$Y/\mu$	Element	$Y/\mu$	Element	$Y/\mu$
3 Li	2.72	38 Sr	(2.71) <sup>a</sup>	65 Tb	2.52
4 Be	2.08	39 Y	2.51	66 Dy	2.49
5 B	2.17	40 Zr	2.70	67 Ho	2.52
6 C(g)	2.56	41 Nb	2.80	68 Er	2.48
6 C(d)	2.50	42 Mo	2.83	69 Tm	(2.48) <sup>a</sup>
11 Na	2.61	43 Tc	(2.59) <sup>a</sup>	70 Yb	2.56
12 Mg	2.55	44 Ru	2.58	71 Lu	(2.50) <sup>a</sup>
13 Al	2.67	45 Rh	2.53	72 Hf	2.59
14 Si	2.59	46 Pd	2.42	73 Ta	2.64
15 P(w, r, b)	(2.67) <sup>a</sup>	47 Ag	2.82	74 W	2.60
16 S(r)	2.69	48 Cd	2.58	75 Re	2.58
19 K	2.78	49 In	2.82	76 Os	(2.57) <sup>a</sup>
20 Ca	2.67	50 Sn(g)	2.84	77 Ir	2.51
21 Sc	(2.54) <sup>a</sup>	50 Sn(w)	2.64	78 Pt	2.80
22 Ti	2.69	51 Sb	2.74	79 Au	2.83
23 V	2.83	52 Te	2.68	80 Hg	2.74
24 Cr	2.08	55 Cs	(2.71) <sup>a</sup>	81 Tl	2.89
25 Mn	2.59	56 Ba	2.58	82 Pb	2.91
26 Fe	2.58	57 La	2.55	83 Bi	2.66
27 Co	2.70	58 Ce( $\alpha$ )	2.31	84 Po	(2.68) <sup>a</sup>
28 Ni	2.58	58 Ce( $\gamma$ )	2.51	87 Fr	(2.71) <sup>a</sup>
29 Cu	2.74	59 Pr	2.41	88 Ra	(2.61) <sup>a</sup>
30 Zn	2.48	60 Nd	2.62	89 Ac	(2.54) <sup>a</sup>
31 Ga	2.47	61 Pm	(2.53) <sup>a</sup>	90 Th	2.68
32 Ge	2.52	62 Sm	2.70	91 Pa	(2.56) <sup>a</sup>
33 As	(2.67) <sup>a</sup>	63 Eu	(2.58) <sup>a</sup>	92 U	2.53
34 Se	(2.68) <sup>a</sup>	64 Gd	2.52	93 Np	(2.51) <sup>a</sup>
37 Rb	(2.71) <sup>a</sup>			94 Pu	2.21

<sup>a</sup> Estimated value; see text for further discussion.

the values of  $Y$  and  $\mu$  given in Tables I and II, respectively. The mean value for all of the experimental data is  $2.60 \pm 0.17$ , which is identical to that calculated from the mean value of Poisson's ratio. The error,  $\pm 0.17$ , corresponds to a percentage error of  $\pm 6.5$ , which is misleadingly small. If Poisson's ratio and the corresponding error were to be calculated from the above numbers, it would be found that  $\sigma = 0.300 \pm 0.080$ . This error is equivalent to a percentage error of  $\pm 26.7$ . The ratio  $Y/\mu$  varies from a minimum of 2.08 for beryllium and chromium to a maximum of 2.91 for lead, and lies within the minimum and maximum theoretical limits, 2.0 and 3.0.